

# CS 295: Optimal Control and Reinforcement Learning Winter 2020

## Lecture 13: Exploration

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# Today's lecture

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- Sparse and dense rewards
- Sandbox for exploration vs. exploitation: Multi-Armed Bandits (MAB)
- Count-based exploration
- Thompson sampling

# Relation between RL and IL

- Why is RL so much harder than IL?
  - ▶ IL:  $\pi_T(a|s)$  indicates a good action to take in  $s$
  - ▶ RL:  $r(s, a)$  does not indicate a good action,  $Q^*(s, a)$  does but it's nonlocal
- But didn't we see an equivalence between RL and IL?
  - ▶ Isn't  $\nabla_{\theta} \mathbb{E}[\log \pi_{\theta}(a|s)]$  in IL like  $\nabla_{\theta} \mathbb{E}[\log \pi_{\theta}(a|s)R]$  in RL?
  - ▶ Yes, except for the distribution: teacher demonstrations in IL, vs. learner in RL
  - ▶ Can the learner prefer good episodes? Well, that's the entire point...

# IL as dense-reward RL

- In cross-entropy Behavior Cloning we maximize

$$\mathbb{E}_{s,a \sim p_T} [\log \pi_\theta(a|s)] = -\mathbb{D}[\pi_T \parallel \pi_\theta] - \mathbb{H}[\pi_T]$$

- ▶ Like RL, but with teacher distribution and extremely sparse reward  $R = 1_{\text{success}}$
- What if instead we minimize the other KL divergence?

$$\mathbb{D}[\pi_\theta \parallel \pi_T] = -\mathbb{E}_{s,a \sim p_\theta} [\log \pi_T(a|s)] - \mathbb{H}[\pi_\theta]$$

- ▶ This is exactly RL with  $r(s, a) = \log \pi_T(a|s)$  and entropy regularizer
- ▶ Now  $r(s, a)$  does give global information
- ▶ In fact, with deterministic teacher,  $r(s, a) = -\infty$  for any suboptimal action

# Reward shaping

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- One advantage of RL over IL is that rewards can be given programmatically
  - Allowing automatic supervision of many episodes
- Sparse reward functions may be easier to program than dense ones
  - Easier to identify good goal states and safety violations after the fact
- Reward shaping: the practice of adjusting the reward function for easier RL
  - More art than science, partly because "easy to program" is hard to quantify
- General tips:
  - Reward "bottleneck states": subgoals that are likely to help the bigger goals
  - To guide exploration, break down long sequences of coordinated actions
    - e.g. place reward beacons on long narrow paths, such that exploration from each can stumble on next

# Learning with sparse rewards

- Montezuma's Revenge

- ▶ Key = 100 points

- ▶ Door = 500 points

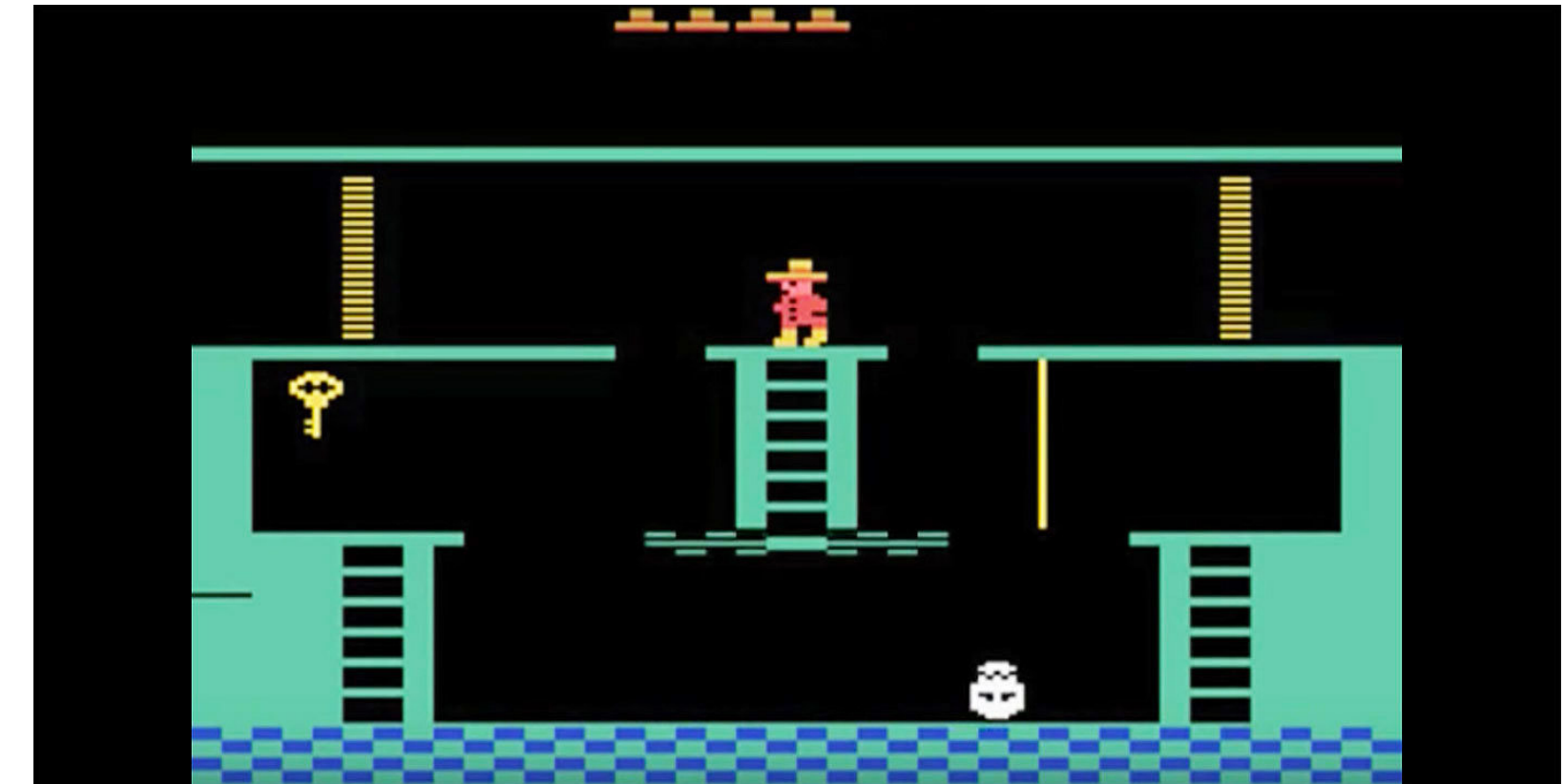
- ▶ Skull = 0 points

- Is it good? Bad? Does something off-screen? Opens up an easter egg?

- ▶ Humans have a head start with transfer from known objects

- Exploration before learning:

- ▶ Random walk until you get some points — could take a while!



# Optimal exploration in simplified settings

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- Multi-Arm Bandits (MAB): single state, one-step horizon
  - Exploration–exploitation tradeoff very well understood
- Contextual bandits: random state, one-step horizon
  - Also has good theory; part of the exciting field of Online Learning
- Tabular RL
  - Some good heuristics, recent theoretical guarantees
- Deep RL
  - Only few exploratory ideas and heuristics



# Multi-Arm Bandits (MABs)

- "One-arm bandit":

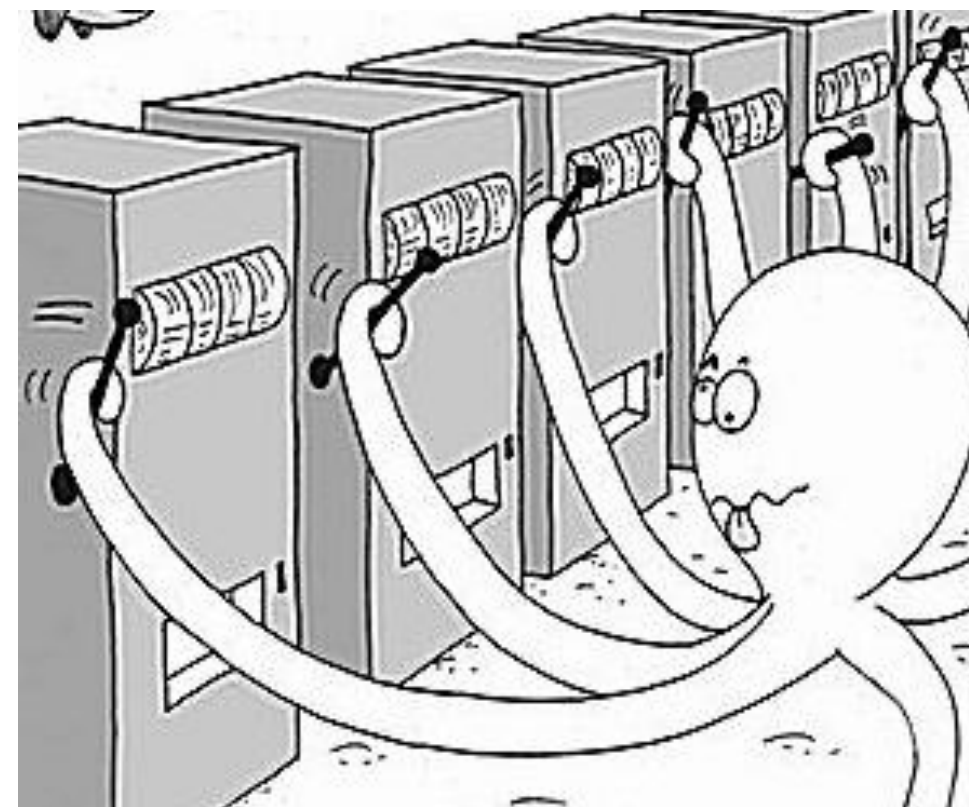
- Multi-arm bandit:

- States:  $\{s_0\}$

- Actions:  $\{\text{pull}_1, \dots, \text{pull}_k\}$

- One-step, no transitions

- Rewards:  $p(r|\text{pull}_i)$





# Let's play!

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- <http://iosband.github.io/2015/07/28/Beat-the-bandit.html>

# Exploration vs. exploitation

- We can choose actions that seemed good so far (exploitation)
- But we could be missing out on even better ones (exploration)
- Algorithms we saw before would try everything enough times — trivial
- What if we care about rewards while we learn
- Regret: how much worse our return is than an optimal action

$$\rho(T) = T \mathbb{E}[r|a^*] - \sum_{t=0}^{T-1} r_t$$

- Can we get the regret to grow sub-linearly with  $T$ ; average regret tends to 0

# Optimism under uncertainty

- Let's be more conservative than  $E^3$  in our optimism
- Track the mean reward for each arm  $\hat{\mu}_i = \frac{1}{N_i} \sum_{t_i} r_{t_i}$
- By the central limit theorem, the distribution of  $\hat{\mu}_i$  tends quickly to Gaussian
  - with standard deviation  $O\left(\frac{1}{\sqrt{N_i}}\right)$
- Let's be optimistic by a slowly-growing number of standard deviations
$$a = \operatorname{argmax}_i \hat{\mu}_i + \sqrt{\frac{2 \ln T}{N_i}}$$
  - Has to grow because we don't know the constant in the variance
  - But not too fast, or we fail to exploit what we do know
- Regret:  $\rho(T) = O(\log T)$ , provably optimal

# Learning as POMDP planning

- We can frame the learning problem as a POMDP planning problem
- Extend the state with the model parameters  $\tilde{s}_t = (s_t, \theta)$ 
  - Uncontrollable, unobservable
- Now we "know" the dynamics:  $p((s', \theta) | (s, \theta), a) = p_\theta(s' | s, a)$
- For the rewards:  $p(r | (s, \theta), a) = p_\theta(r | s, a)$
- This is a special case of POMDP planning
  - POMDP planning in parameter state space is at least as hard as MDP learning
  - Too hard to solve with POMDP methods, even in the bandits case

# Thompson sampling

- In the bandits case:  $p_{\theta_i}(r|a_i)$
- Consider the belief = posterior over  $\theta$  (note: distribution over distributions)
- Computing the belief value function: optimal experiment design; challenging
- Approximation:
  - Sample  $\theta|(a_t, r_t)_t \sim b_t$  from the belief
  - Take the optimal action
  - Update the belief
  - Repeat



# RL exploration is more complicated...

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- Need to consider states and dynamics
- Need coordinated behavior to get *anywhere*
  - Cross a bridge to get the game started
  - Random exploration will kill us with high probability
    - Structured exploration
- How to define regret?
  - With respect to constant action? We can outperform it
  - With respect to optimal policy? May be too hard to learn, linear regret
  - Most approaches are heuristic, no regret guarantees

# Count-based exploration

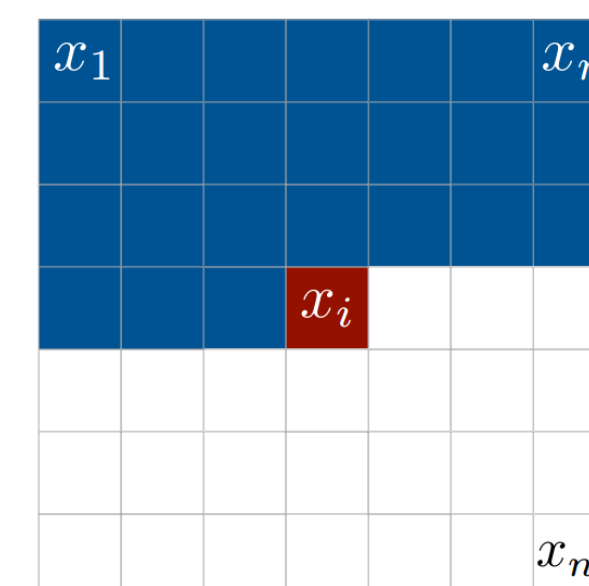
- Generalizing  $a = \operatorname{argmax}_i \hat{\mu}_i + \sqrt{\frac{2 \ln T}{N_i}}$  to RL
- Count visitations to each state  $N(s)$  (or state-action  $N(s, a)$ )
- Optimism under uncertainty, add exploration bonus to scarcely-visited states

$$\tilde{r} = r + r_e(N(s))$$

- $r_e$  should be monotonic decreasing in  $N(s)$
- Need to tune its weight

# Density model for count-based exploration

- How to represent "counts" in large state spaces?
  - We may never see the same state twice
  - If a state is very similar to ones we've seen often, is it new?
- Train a density model  $p_\phi(s)$  over past experience
- Unlike generative models, we care about getting the density correctly
  - But not about the quality of samples
- Density models for images:
  - CTS, PixelRNN, PixelCNN, etc.



# Pseudo-counts

- How to infer pseudo-counts from a density model?

$$p_{\phi}(s) = \frac{N(s)}{N}$$

- After another visit:

$$p_{\phi'}(s) = \frac{N(s)+1}{N+1}$$

- To recover the pseudo-count:

- $p_{\phi'} \leftarrow$  mock-update the density model with another visit of  $s$

- Compute  $\hat{N} = \frac{1-p_{\phi'}(s)}{p_{\phi'}(s)-p_{\phi}(s)}p_{\phi}(s)$        $\hat{N}(s) = \hat{N}p_{\phi}(s)$

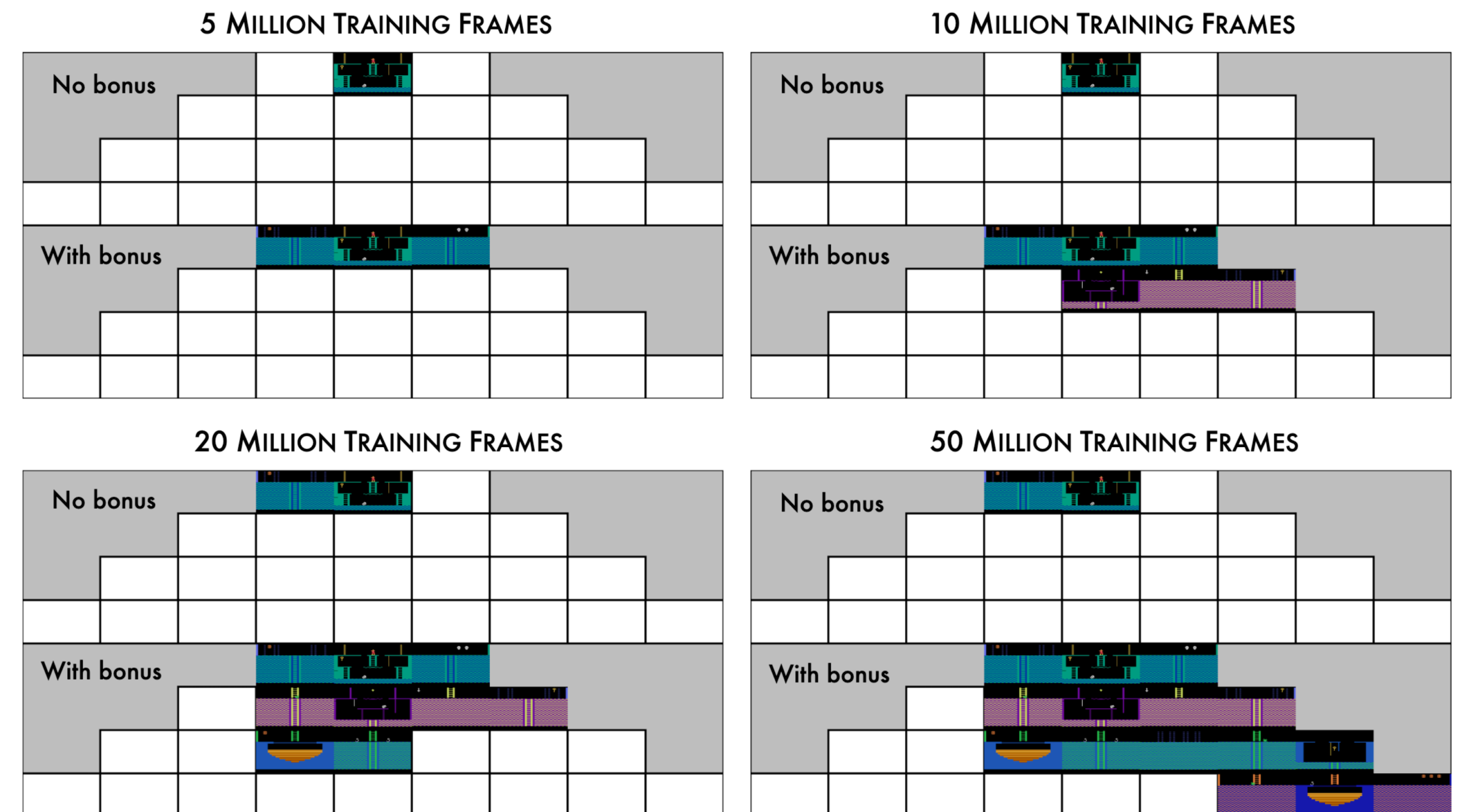
# Exploration bonus

- What's a good exploration bonus?

- In bandits: Upper Confidence Bound (UCB)  $r_e(N(s)) = \sqrt{\frac{2 \ln N}{N(s)}}$

- In RL, often:  $r_e(N(s)) = \sqrt{\frac{1}{N(s)}}$

- [Bellemare et al., 2016]:





# Thompson sampling for RL

- Keep a distribution over models
- What's our model?
  - MDP
  - Q-function
- Sample  $Q \sim p_\theta$
- Roll out an episode with the greedy policy  $\pi = \operatorname{argmax}_a Q$
- Use experience to update  $p(Q)$
- Repeat

# Recap

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- Dense rewards help, but hard to generate
- Challenges of random exploration can be overcome with
  - Count-based exploration bonus for novelty, effective way to make rewards denser
  - Posterior sampling for coordinated exploration actions